Package ‘gld’

February 19, 2015

Version 2.2.1
Date 2014/02/19
Title Estimation and use of the generalised (Tukey) lambda distribution
Depends stats
Suggests graphics, lmom, e1071
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Description The generalised lambda distribution, or Tukey lambda distribution, provides a wide variety of shapes with one functional form. This package provides random numbers, quantiles, probabilities, densities for four different parameterisations of the distribution. It provides the density function, distribution function and Quantile-Quantile plots. It implements a variety of estimation methods for the distribution, including diagnostic plots. Estimation methods include the starship (all 4 parameterisations) and a number of methods for only the FKML parameterisation. These include maximum likelihood, maximum product of spacings, Titterington’s method, L moments, Trimmed L moments and Distributional Least Absolutes.
License GPL (>= 2)
NeedsCompilation yes
Repository CRAN
Date/Publication 2014-02-19 07:39:51

R topics documented:

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fit.fkml

Estimate parameters of the FKML parameterisation of the generalised lambda distribution

Description

Estimates parameters of the FKML parameterisation of the Generalised \( \lambda \) Distribution. Five estimation methods are available; Numerical Maximum Likelihood, Maximum Product of Spacings, Titterington’s Method, the Starship (also available in the \texttt{starship} function, which uses the same underlying code as this for the \texttt{fkml} parameterisation), and Trimmed L-Moments.

Usage

\begin{verbatim}
fit.fkml(x, method = "ML", t1 = 0, t2 = 0,
        l3.grid = c(-0.9, -0.5, -0.1, 0, 0.1, 0.2, 0.4, 0.8, 1, 1.5),
        l4.grid = l3.grid, record.cpu.time = TRUE, optim.method = "Nelder-Mead",
        inverse.eps = .Machine$double.eps, optim.control=list(maxit=10000),
        optim.penalty=1e20, return.data=FALSE)
\end{verbatim}

Arguments

<table>
<thead>
<tr>
<th>Argument</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>( x )</td>
<td>Data to be fitted, as a vector</td>
</tr>
<tr>
<td>\texttt{method}</td>
<td>A character string, to select the estimation method. One of: \texttt{ML} for Numerical Maximum Likelihood, \texttt{MPS} or \texttt{MSP} for Maximum Product of Spacings, \texttt{TM} for Titterington’s Method, \texttt{SM} for Starship Method, \texttt{TL} for Method of TL-moments, or DLA for the method of distributional least absolutes.</td>
</tr>
<tr>
<td>( t1 )</td>
<td>Number of observations to be trimmed from the left in the conceptual sample, ( t_1 ) (A non-negative integer, only used by TL-moment estimation, see details section)</td>
</tr>
<tr>
<td>( t2 )</td>
<td>Number of observations to be trimmed from the right in the conceptual sample, ( t_2 ) (A non-negative integer, only used by TL-moment estimation, see details section). These two arguments are restricted by ( t_1 + t_2 &lt; n ), where ( n ) is the sample size</td>
</tr>
<tr>
<td>\texttt{l3.grid}</td>
<td>A vector of values to form the grid of values of ( \lambda_3 ) used to find a starting point for the optimisation.</td>
</tr>
<tr>
<td>\texttt{l4.grid}</td>
<td>A vector of values to form the grid of values of ( \lambda_4 ) used to find a starting point for the optimisation.</td>
</tr>
</tbody>
</table>
**record.cpu.time**

Boolean — should the CPU time used in fitting be recorded in the fitted model object?

**optim.method**

Optimisation method, use any of the options available under method of optim.

**inverse.eps**

Accuracy of calculation for the numerical determination of $F(x)$, defaults to .Machine$\cdot$double.eps.

**optim.control**

List of options for the optimisation step. See optim for details.

**optim.penalty**

The penalty to be added to the objective function if parameter values are proposed outside the allowed region

**return.data**

Logical: Should the function return the data (from the argument data)?

---

**Details**

Maximum Likelihood Estimation of the generalised lambda distribution (gld) proceeds by calculating the density of the data for candidate values of the parameters. Because the gld is defined by its quantile function, the method first numerically obtains $F(x)$ by inverting $Q(u)$, then obtains the density for that observation.

Maximum Product of Spacings estimation (sometimes referred to as Maximum Spacing Estimation, or Maximum Spacings Product) finds the parameter values that maximise the product of the spacings (the difference between successive depths, $F_{\theta}(x_{(i+1)}) - F_{\theta}(x_{(i)})$, where $F_{\theta}(x)$ is the distribution function for the candidate values of the parameters). See Dean (2013) and Cheng & Amin (1981) for details.

Titterington (1985) remarked that MPS effectively added an “extra observation”; there are $N$ data points in the original sample, but $N + 1$ spacings in the expression maximised in MPS. Instead of using spacings between transformed data points, method TM uses spacings between transformed, adjacently-averaged, data points. The spacings are given by $D_i = F_{\theta}(z_{(i)}) - F_{\theta}(z_{(i-1)})$, where $\alpha_1 = z_0 < z_1 < \ldots < z_n = \alpha_2$ and $z_i = (x_{(i)} + x_{(i+1)})/2$ for $i = 1, 2, \ldots, n-1$ (where $\alpha_1$ and $\alpha_2$ are the lower and upper bounds on the support of the distribution). This reduces the number of spacings to $n$ and achieves concordance with the original sample size. See Titterington (1985) and Dean (2013) for details.

The starship is built on the fact that the $g\lambda d$ is a transformation of the uniform distribution. Thus the inverse of this transformation is the distribution function for the gld. The starship method applies different values of the parameters of the distribution to the distribution function, calculates the depths $q$ corresponding to the data and chooses the parameters that make these calculated depths closest (as measured by the Anderson-Darling statistic) to a uniform distribution. See King & MacGillivray (1999) for details.

TL-Moment estimation chooses the values of the parameters that minimise the difference between the sample Trimmed L-Moments of the data and the Trimmed L-Moments of the fitted distribution. TL-Moments are based on inflating the conceptual sample size used in the definition of L-Moments. The $t_1$ and $t_2$ arguments to the function define the extent of trimming of the conceptual sample. Thus, the default values of $t_1=0$ and $t_2=0$ reduce the TL-Moment method to L-Moment estimation. $t_1$ and $t_2$ give the number of observations to be trimmed (from the left and right respectively) from the conceptual sample of size $n + t_1 + t_2$. These two arguments should be non-negative integers, and $t_1 + t_2 < n$, where $n$ is the sample size. See Elamir and Seheult (2003) for more on TL-Moments in general, Asquith, (2007) for TL-Moments of the RS parameterisation of the gld and Dean (2013) for more details on TL-Moment estimation of the gld.
The method of distributional least absolutes (DLA) minimises the sum of absolute deviations between the order statistics and their medians (based on the candidate parameters). See Dean (2013) for more information.

Value

fit.fkml returns an object of class "starship" (regardless of the estimation method used).

print prints the estimated values of the parameters, while summary.starship prints these by default, but can also provide details of the estimation process (from the components grid.results, data and optim detailed below).

The value of fit.fkml is a list containing the following components:

lambda A vector of length 4, giving the estimated parameters, in order, $\lambda_1$ - location parameter $\lambda_2$ - scale parameter $\lambda_3$ - first shape parameter $\lambda_4$ - second shape parameter

grid.results output from the grid search

optim output from the optim search, optim for details

cpu A vector showing the computing time used, returned if record.cpu.time is TRUE

data The data, if return.data is TRUE

Author(s)

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References


See Also

starship Generalised Lambda Distribution
Examples

```r
example.data <- rgl(200,c(3,1,4,-0.1),param="fkml")
example.fit <- fit.fkml(example.data,"MSP",return.data=TRUE)
print(example.fit)
summary(example.fit)
plot(example.fit,one.page=FALSE)
```

Generalised Lambda Distribution

The Generalised Lambda Distribution

Description

Density, quantile density, distribution function, quantile function and random generation for the
generalised lambda distribution (also known as the asymmetric lambda, or Tukey lambda). Provides
for four different parameterisations, the *fmkl* (recommended), the *rs*, the *gpd* and a five parameter
version of the *FMKL*, the *fm5*.

Usage

```r
dgl(x, lambda1 = 0, lambda2 = NULL, lambda3 = NULL, lambda4 = NULL,
   param = "fkml", lambda5 = NULL, inverse.eps = .Machine$double.eps,
   max.iterations = 500)
dqgl(p, lambda1, lambda2 = NULL, lambda3 = NULL, lambda4 = NULL,
   param = "fkml", lambda5 = NULL)
qdgl(p, lambda1, lambda2 = NULL, lambda3 = NULL, lambda4 = NULL,
   param = "fkml", lambda5 = NULL)
pgl(q, lambda1 = 0, lambda2 = NULL, lambda3 = NULL, lambda4 = NULL,
   param = "fkml", lambda5 = NULL, inverse.eps = .Machine$double.eps,
   max.iterations = 500)
qgl(p, lambda1, lambda2 = NULL, lambda3 = NULL, lambda4 = NULL,
   param = "fkml", lambda5 = NULL)
rgl(n, lambda1=0, lambda2 = NULL, lambda3 = NULL, lambda4 = NULL,
   param = "fkml", lambda5 = NULL)
```

Arguments

- `x,q` vector of quantiles.
- `p` vector of probabilities.
- `n` number of observations.
- `lambda1` This can be either a single numeric value or a vector.

If it is a vector, it must be of length 4 for parameterisations *fmkl*, *rs* and *gpd* and
of length 5 for parameterisation *fm5*. If it is a vector, it gives all the parameters of
the generalised lambda distribution (see below for details) and the other `lambda`
arguments must be left as NULL.
The generalised lambda distribution, also known as the asymmetric lambda, or Tukey lambda distribution, is a distribution with a wide range of shapes. The distribution is defined by its quantile function (Q(u)), the inverse of the distribution function. The glD package implements three parameterisations of the distribution. The default parameterisation (the FMKL) is that due to Freimer, Mudholkar, Kollia and Lin (1988) (see references below), with a quantile function:

\[ Q(u) = \lambda_1 + \frac{u^{\lambda_3} - 1}{\lambda_3} - \frac{(1-u)^{\lambda_4} - 1}{\lambda_4} \]

for \( \lambda_2 > 0 \).

A second parameterisation, the RS, chosen by setting param="rs" is that due to Ramberg and Schmeiser (1974), with the quantile function:

\[ Q(u) = \lambda_1 + \frac{u^{\lambda_3} - (1-u)^{\lambda_4}}{\lambda_2} \]

This parameterisation has a complex series of rules determining which values of the parameters produce valid statistical distributions. See gl.check.lambda for details.

Another parameterisation, the GPD, chosen by setting param="gpd" is due to van Staden and Loots (2009), with a quantile function:

\[ Q(u) = \alpha + \beta((1 - \delta)\frac{(u^\lambda - 1)}{\lambda} - \delta((1 - u)^\lambda - 1)) \]

for \( \beta > 0 \) and \( 0 \leq \delta \leq 1 \). (where the parameters appear in the par argument to the function in the order \( \alpha, \beta, \delta, \lambda \)). This parameterisation has simpler L-moments than other parameterisations and \( \delta \) is a skewness parameter and \( \lambda \) is a tailweight parameter.
Another parameterisation, the FM5, chosen by setting \texttt{param="fm5"} adds an additional skewing parameter to the FMKL parameterisation. This uses the same approach as that used by Gilchrist (2000) for the RS parameterisation. The quantile function is

\[ F^{-1}(u) = \lambda_1 + \frac{\frac{(1-\lambda_2)(u^{\lambda_3}-1)}{\lambda_3} - \frac{(1+\lambda_5)((1-u)^{\lambda_4}-1)}{\lambda_4}}{\lambda_2} \]

for \( \lambda_2 > 0 \) and \(-1 \leq \lambda_5 \leq 1\).

The distribution is defined by its quantile function and its distribution and density functions do not exist in closed form. Accordingly, the results from \texttt{pgl} and \texttt{dgl} are the result of numerical solutions to the quantile function, using the Newton-Raphson method. Since the quantile density function, \( f(F^{-1}(u)) \), does exist, an additional function, \texttt{qdgl}, computes this.

The functions \texttt{qdgl.fmkl}, \texttt{qdgl.rs}, \texttt{qdgl.fm5}, \texttt{qgl.fmkl}, \texttt{qgl.rs} and \texttt{qgl.fm5} from versions 1.5 and earlier of the gld package have been renamed (and hidden) to \texttt{.qdgl.fmkl}, \texttt{.qdgl.rs}, \texttt{.qdgl.fm5}, \texttt{.qgl.fmkl}, \texttt{.qgl.rs} and \texttt{.qgl.fm5} respectively. See the code for more details.

### Value

- \texttt{dgl} gives the density (based on the quantile density and a numerical solution to \( F^{-1}(u) = x \)),
- \texttt{qdgl} gives the quantile density,
- \texttt{pgl} gives the distribution function (based on a numerical solution to \( F^{-1}(u) = x \)),
- \texttt{qgl} gives the quantile function, and
- \texttt{rgl} generates random deviates.

### Author(s)

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### References


\url{http://tolstoy.newcastle.edu.au/~rking/gld/}
Examples

```r
qgl(seq(0,1,0.02),0,1,0.123,-4.3)
pgl(seq(-2,2,0.2),0,1,-1,-2,param="fmkl",inverse.eps=1e-10)
rgl(21,c(3,2,0.3,-0.1),param="gpd")
```

# calculate the probabilities less accurately than normal

---

**gl.check.lambda**  
*Function to check the validity of parameters of the generalized lambda distribution*

---

**Description**

Checks the validity of parameters of the generalized lambda. The tests are simple for the FMKL, FM5 and GPD parameterisations, and much more complex for the RS parameterisation.

**Usage**

```r
gl.check.lambda(lambdasL lambdaR = NULLL lambdaS = NULLL lambdaT = NULLL param = BfkmlBL
lambdaU = nullL vect = false)
```

**Arguments**

- `lambdas`  
  - This can be either a single numeric value or a vector.  
  - If it is a vector, it must be of length 4 for parameterisations fmkl or rs and of length 5 for parameterisation fm5. If it is a vector, it gives all the parameters of the generalised lambda distribution (see below for details) and the other lambda arguments must be left as NULL.  
  - If it is a single value, it is \( \lambda_1 \), the location parameter of the distribution and the other parameters are given by the following arguments  
  
  *Note that the numbering of the \( \lambda \) parameters for the fmkl parameterisation is different to that used by Freimer, Mudholkar, Kollia and Lin.*

- `lambda2`  
  - \( \lambda_2 \) - scale parameter

- `lambda3`  
  - \( \lambda_3 \) - first shape parameter

- `lambda4`  
  - \( \lambda_4 \) - second shape parameter

- `lambda5`  
  - \( \lambda_5 \) - a skewing parameter, in the fm5 parameterisation

- `param`  

- `vect`  
  - A logical, set this to TRUE if the parameters are given in the vector form (it turns off checking of the format of lambdas and the other lambda arguments
Details

See GeneralisedLambdaDistribution for details on the generalised lambda distribution. This function determines the validity of parameters of the distribution.

The FMKL parameterisation gives a valid statistical distribution for any real values of $\lambda_1$, $\lambda_3$, $\lambda_4$ and any positive real values of $\lambda_2$.

The FM5 parameterisation gives statistical distribution for any real values of $\lambda_1$, $\lambda_3$, $\lambda_4$, any positive real values of $\lambda_2$ and values of $\lambda_5$ that satisfy $-1 \leq \lambda_5 \leq 1$.

The GPD type gives a valid distribution for any real values of $\alpha$ and $\lambda$, any positive real values of $\beta$ and values of $\delta$ that satisfy $0 \leq \delta \leq 1$.

For the RS parameterisation, the combinations of parameters value that give valid distributions are the following (the region numbers in the table correspond to the labelling of the regions in Ramberg and Schmeiser (1974) and Karian, Dudewicz and McDonald (1996)):

<table>
<thead>
<tr>
<th>region</th>
<th>$\lambda_1$</th>
<th>$\lambda_2$</th>
<th>$\lambda_3$</th>
<th>$\lambda_4$</th>
<th>note</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>all</td>
<td>$&lt; 0$</td>
<td>$&lt; -1$</td>
<td>$&gt; 1$</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>all</td>
<td>$&lt; 0$</td>
<td>$&gt; 1$</td>
<td>$&lt; -1$</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>all</td>
<td>$&gt; 0$</td>
<td>$\geq 0$</td>
<td>$\geq 0$</td>
<td>one of $\lambda_3$ and $\lambda_4$ must be non-zero</td>
</tr>
<tr>
<td>4</td>
<td>all</td>
<td>$&lt; 0$</td>
<td>$\leq 0$</td>
<td>$\leq 0$</td>
<td>one of $\lambda_3$ and $\lambda_4$ must be non-zero</td>
</tr>
<tr>
<td>5</td>
<td>all</td>
<td>$&lt; 0$</td>
<td>$&gt;-1$ and $&lt; 0$</td>
<td>$&gt; 1$</td>
<td>equation 1 below must also be satisfied</td>
</tr>
<tr>
<td>6</td>
<td>all</td>
<td>$&lt; 0$</td>
<td>$&gt; 1$</td>
<td>$&gt;-1$ and $&lt; 0$</td>
<td>equation 2 below must also be satisfied</td>
</tr>
</tbody>
</table>

Equation 1

\[
\frac{(1 - \lambda_3)^{1-\lambda_3}(\lambda_4 - 1)^{\lambda_4 - 1}}{(\lambda_4 - \lambda_3)^{\lambda_4 - \lambda_3}} \leq -\frac{\lambda_3}{\lambda_4}
\]

Equation 2

\[
\frac{(1 - \lambda_4)^{1-\lambda_4}(\lambda_3 - 1)^{\lambda_3 - 1}}{(\lambda_3 - \lambda_4)^{\lambda_3 - \lambda_4}} \leq -\frac{\lambda_4}{\lambda_3}
\]

Value

This logical function takes on a value of TRUE if the parameter values given produce a valid statistical distribution and FALSE if they don’t.

Note

The complex nature of the rules in this function for the RS parameterisation are the reason for the invention of the FMKL parameterisation and its status as the default parameterisation in the other generalized lambda functions.

Author(s)

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References


http://tolstoy.newcastle.edu.au/~rking/gld/

See Also

The generalized lambda functions `GeneralisedLambdaDistribution`

Examples

```r
gl.check.lambda(c(0,1,.23,4.5),vect=TRUE) ## TRUE
gl.check.lambda(c(0,-1,.23,4.5),vect=TRUE) ## FALSE
gl.check.lambda(c(0,1,.05,-0.5),param="rs",vect=TRUE) ## FALSE
gl.check.lambda(c(0,2,1,3.4,1.2),param="fm5",vect=TRUE) ## FALSE
```

Description

Plots to compare estimated Generalised Lambda Distribution parameters to data. This works for the fitted objects created by `starship` and `fit.fkml`.

Usage

```r
## S3 method for class 'starship'
plot(x, data, ask = FALSE, one.page = TRUE,
     breaks = "Sturges", histogram.title = NULL,...)
```

Arguments

- **x**: An object of class `starship`.
- **data**: Data to which the gld was fitted. Leave this as NULL if the return.data argument was TRUE in the `starship` call that created x.
- **ask**: Ask for user input before next plot — passed to `par(ask)`. Does not permanently change this setting. Ignored if `one.page` is TRUE.
- **one.page**: Put the two plots on one page using `par(mfrow=c(2,1))`. Does not permanently change this setting.
plotgl

breaks Control the number of histogram bins — passed to hist.
histogram.title Main title for histogram — passed to hist(main=).
... arguments passed to plot AND hist

Details

summary Gives the details of the starship.adaptivegrid and optim steps.
The class is named starship, after the first estimation method implemented in this package, but this plot is available for any estimated generalised lambda parameters.

Author(s)

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References

http://tolstoy.newcastle.edu.au/~rking/gld/

See Also

starship.fit.fkml

Examples

set.seed(2308)
data <- rgl(100,0,1,2)
starship.result <- starship(data,optim.method="Nelder-Mead",initgrid=list(lcvect=(0:4)/10,ldvect=(0:4)/10),return.data=TRUE)
plot(starship.result,one.page=FALSE)

plotgl Plots of density and distribution function for the generalised lambda distribution

Description

Produces plots of density and distribution function for the generalised lambda distribution. Although you could use plot(function(x)dgl(x)) to do this, the fact that the density and quantiles of the generalised lambda are defined in terms of the depth, \( u \), means that a separate function that uses the depths to produce the values to plot is more efficient.
Usage

plotgld(lambda1 = 0, lambda2 = NULL, lambda3 = NULL, lambda4 = NULL, param = "fmkl", lambda5 = NULL, add = NULL, truncate = 0, 
bnw = FALSE, col.or.type = 1, granularity = 10000, xlab = "x", 
ylab = NULL, quant.probs = seq(0,1,.25), new.plot = NULL, ...
plotglc(lambda1 = 0, lambda2 = NULL, lambda3 = NULL, lambda4 = NULL, param = "fmkl", lambda5 = NULL, granularity = 10000, xlab = "x", 
ylab = "cumulative probability", add = FALSE, ...)

Arguments

lambda1 This can be either a single numeric value or a vector.
If it is a vector, it must be of length 4 for parameterisations fmkl or rs and of
length 5 for parameterisation fm5. If it is a vector, it gives all the parameters of
the generalised lambda distribution (see below for details) and the other lambda
arguments must be left as NULL.
If it is a a single value, it is λ₁, the location parameter of the distribution and the
other parameters are given by the following arguments
Note that the numbering of the λ parameters for the fmkl parameterisation is
different to that used by Freimer, Mudholkar, Kollia and Lin.

lambda2 λ₂ - scale parameter
lambda3 λ₃ - first shape parameter
lambda4 λ₄ - second shape parameter
lambda5 λ₅ - a skewing parameter, in the fm5 parameterisation
param choose parameterisation: fmkl uses Freimer, Mudholkar, Kollia and Lin (1988)
(default). rs uses Ramberg and Schmeiser (1974) fm5 uses the 5 parameter
version of the FMKL parameterisation (paper to appear)
add a logical value describing whether this should add to an existing plot (using
lines) or produce a new plot (using plot). Defaults to FALSE (new plot) if
both add and new.plot are NULL.
truncate for plotgld, a minimum density value at which the plot should be truncated.
bnw a logical value, true for a black and white plot, with different densities identified
using line type (lty), false for a colour plot, with different densities identified
using line colour (col)
col.or.type Colour or type of line to use
granularity Number of points to calculate quantiles and density at — see details
xlab X axis label
ylab Y axis label
quant.probs Quantiles of distribution to return (see value below). Set to NULL to suppress
this return entirely.
new.plot a logical value describing whether this should produce a new plot (using plot),
or add to an existing plot (using lines). Ignored if add is set.
... arguments that get passed to plot if this is a new plot
Details

The generalised lambda distribution is defined in terms of its quantile function. The density of the distribution is available explicitly as a function of depths, $u$, but not explicitly available as a function of $x$. This function calculates quantiles and depths as a function of depths to produce a density plot plotgld or cumulative probability plot plotglc.

The plot can be truncated, either by restricting the values using xlim — see par for details, or by the truncate argument, which specifies a minimum density. This is recommended for graphs of densities where the tail is very long.

Value

A number of quantiles from the distribution, the default being the minimum, maximum and quartiles.

Author(s)

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References


http://tolstoy.newcastle.edu.au/~rking/gld/

See Also

GeneralisedLambdaDistribution

Examples

plotgld(0,1.4640474,.1349,.1349,main="Approximation to Standard Normal", sub="But you can see this isn’t on infinite support")
plotgld(1.42857143,1,.7,.3,main="The whale")
plotglda(0,-1.5,-0.3,param="rs")
plotgldc(0,-1.5,-0.3,param="rs",xlim=c(1,2))
# A bizarre shape from the RS parameterisation
plotgld(0,1.5,-0.3,param="fmkl")
plotgld(10/3,1,.3,-1,truncate=1e-3)

plotgld(0,1,.0742,.0742,col.or.type=2,param="rs", main="All distributions have the same moments", sub="The full range of all distributions is shown")
plotgld(0,1.6.026,6.026,col.or.type=3,new.plot=FALSE,param="rs")
# An illustration of problems with moments as a method of characterising shape

```
plotgld(0, 1, 3.5, 2.97, col.or.type=4, new.plot=FALSE, param="rs")
legend(0.25, 3.5, lty=1, col=c(2, 3, 4), legend=c("(0, 1, 0.042, 0.072)",
"(0, 1, 6.026, 6.026)", "(0, 1, 3.5498, 2.297)"), cex=0.9)
```

---

**print.starship**

Print (or summarise) the results of estimation of Generalised Lambda Distribution

---

**Description**

Print (or summarise) the results of estimation of the parameters of the Generalised Lambda Distribution, from either starship or fit.fkml

**Usage**

```r
## S3 method for class 'starship'
summary(object, ...)

## S3 method for class 'starship'
print(x, digits = max(3, getOption("digits") - 3), ...)
```

**Arguments**

- `x` An object of class starship.
- `object` An object of class starship.
- `digits` minimal number of significant digits, see print.default.
- `...` arguments passed to print

**Details**

summary Gives the details of the starship.adaptivegrid and optim steps.

The class is named starship, after the first estimation method implemented in this package, but is used for any estimated generalised lambda parameters.

**Author(s)**


Darren Wraith
qqgl

References


http://tolstoy.newcastle.edu.au/~rking/gld/

See Also

starship, starship.adaptivegrid, starship.obj

Examples

data <- rgl(100,0,1,2,2)
starship.result <- starship(data, optim.method="Nelder-Mead", initgrid=list(lcvect=c(0:4)/10, ldvect=c(0:4)/10))
print(starship.result)
summary(starship.result, estimation.details=TRUE)

qqgl

*Quantile-Quantile plot against the generalised lambda distribution*

Description

qqgl produces a Quantile-Quantile plot of data against the generalised lambda distribution, or a Q-Q plot to compare two sets of parameter values for the generalised lambda distribution. It does for the generalised lambda distribution what qqnorm does for the normal.

Usage

```r
qqgl(y = NULL, lambda1 = 0, lambda2 = NULL, lambda3 = NULL, lambda4 = NULL,
     param = "fkml", lambda5 = NULL, abline = TRUE, lambda.pars1 = NULL, lambda.pars2 = NULL,
     param2 = "fkml", points.for.2.param.sets = 4000, ...)
```

Arguments

- `y`: The data sample
- `lambda1`: This can be either a single numeric value or a vector. If it is a vector, it must be of length 4 for parameterisations `fkml` or `rs` and of length 5 for parameterisation `fm5`. If it is a vector, it gives all the parameters of the generalised lambda distribution (see below for details) and the other `lambda` arguments must be left as NULL.
Alternatively, leave \( \lambda_1 \) as the default value of 0 and use the \( \text{lambda.pars1} \) argument instead.

If it is a a single value, it is \( \lambda_1 \), the location parameter of the distribution and the other parameters are given by the following arguments

_Note that the numbering of the \( \lambda \) parameters for the fmkl parameterisation is different to that used by Freimer, Mudholkar, Kollia and Lin._

| \( \lambda_2 \) | - scale parameter |
| \( \lambda_3 \) | - first shape parameter |
| \( \lambda_4 \) | - second shape parameter |
| \( \lambda_5 \) | - a skewing parameter, in the fm5 parameterisation |

\( \text{param} \) _choose parameterisation: fmkl uses Freimer, Mudholkar, Kollia and Lin (1988) (default). \( \text{rs} \) uses Ramberg and Schmeiser (1974) \( \text{fm5} \) uses the 5 parameter version of the FMKL parameterisation (paper to appear)_

\( \text{abline} \) _A logical value, TRUE adds a line through the origin with a slope of 1 to the plot_

\( \text{lambda.pars1} \) _Parameters of the generalised lambda distribution (see \( \lambda_1 \) to \( \lambda_4 \) for details.)_

\( \text{lambda.pars2} \) _Second set of parameters of the generalised lambda distribution (see \( \lambda_1 \) to \( \lambda_4 \) for details. Use \( \text{lambda.pars1} \) and \( \text{lambda.pars2} \) to produce a QQ plot comparing two generalised lambda distributions_

\( \text{param2} \) _parameterisation to use for the second set of parameter values_

\( \text{points.for.2.param.sets} \) _Number of quantiles to use in a Q-Q plot comparing two sets of parameter values_

\( \ldots \) _graphical parameters, passed to \text{qqplot}_

**Details**

See \text{gld} for more details on the Generalised Lambda Distribution. A Q-Q plot provides a way to visually assess the correspondence between a dataset and a particular distribution, or between two distributions.

**Value**

A list of the same form as that returned by \text{qqline}.

| \( x \) | The \( x \) coordinates of the points that were/would be plotted, corresponding to a generalised lambda distribution with parameters \( \lambda_1, \lambda_2, \lambda_3, \lambda_4 \). |
| \( y \) | The original \( y \) vector, i.e., the corresponding \( y \) coordinates, or a corresponding set of quantiles from a generalised lambda distribution with the second set of parameters |

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References


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See Also
gld, starship

Examples

```r
qqgl(rgl100,0,1,0,−1),0,1,0,−1)
qqgl(lambda1=c(0,0.01,0.01),lambda.pars2=c(0,.01,0.01),param2="rs",pch=".")
```

starship Carry out the “starship” estimation method for the generalised lambda distribution

Description

Estimates parameters of the generalised lambda distribution on the basis of data, using the starship method. The starship method is built on the fact that the generalised lambda distribution (gld) is a transformation of the uniform distribution. This method finds the parameters that transform the data closest to the uniform distribution. This function uses a grid-based search to find a suitable starting point (using starship.adaptivegrid) then uses optim to find the parameters that do this. For the fkml parameterisation, this function calls fit.fkml to estimate.

Usage

```r
starship(data, optimNmethod = "Nelder-Mead", initgrid = NULL, inverseNeps = .Machine$doubleNeps, param=FMKL, optimNcontrol=NULL, returnNdata=FALSE)
```

Arguments

data Data to be fitted, as a vector

optimNmethod Optimisation method for optim to use, defaults to Nelder-Mead

initgrid Grid of values of λ₃ and λ₄ to try, in starship.adaptivegrid. This should be a list with elements, lcvect, a vector of values for λ₃, ldvect, a vector of values for λ₄ and levect, a vector of values for λ₅ (levect is only required if param is fm5).

If it is left as NULL, the default grid depends on the parameterisation. For fm1, both lcvect and ldvect default to:

-0.9 -0.5 -0.1 0.0 0.1 0.2 0.4 0.8 1 1.5

(levect is NULL).
For rs, both lcvec and ldvec default to:

0.1 0.2 0.4 0.8 1 1.5

(levect is NULL). Note that this restricts the estimates to only part of the region of the $\lambda_3$, $\lambda_4$ plane. It is possible to use this function to obtain starship estimates in the other regions of the plane where the rs parameterisation is valid (see gl.check.lambda for details). Just set the values of initgrid to include those regions.

For gpd, the defaults are: $\delta$:

0.3 0.5 0.7

and $\lambda$:

-1.5 -0.5 0.0 0.2 0.4 0.8 1.5 5

For fm5, both lcvec and ldvec default to:

-1.5 -1 -.5 -0.1 0 0.1 0.2 0.4 0.8 1 1.5

and levect defaults to:

-0.5 0.25 0 0.25 0.5

inverse eps
Accuracy of calculation for the numerical determination of $F(x)$, defaults to .Machine$\cdot$double.eps

param
choose parameterisation: fnk1 uses Freimer, Mudholkar, Kollia and Lin (1988) (default). rs uses Ramberg and Schmeiser (1974) fm5 uses the 5 parameter version of the FMKL parameterisation (paper to appear) gpd uses the van Staden and Loots (2009), or gpd parameterisation.

optim.control
List of options for the optimisation step. See optim for details. If left as NULL, the parscale control is set to scale $\lambda_1$ and $\lambda_2$ by the absolute value of their starting points.

return.data
Logical: Should the function return the data (from the argument data)? Not implemented for fmkl parameterisation

Details

The starship method is described in King & MacGillivray, 1999 (see references). It is built on the fact that the generalised lambda distribution (gld) is a transformation of the uniform distribution. Thus the inverse of this transformation is the distribution function for the gld. The starship method applies different values of the parameters of the distribution to the distribution function, calculates the depths $q$ corresponding to the data and chooses the parameters that make the depths closest to a uniform distribution.

The closeness to the uniform is assessed by calculating the Anderson-Darling goodness-of-fit test on the transformed data against the uniform, for a sample of size length(data).
This is implemented in 2 stages in this function. First a grid search is carried out, over a small number of possible parameter values (see `starship.adaptivegrid` for details). Then the minimum from this search is given as a starting point for an optimisation of the Anderson-Darling value using `optim`, with method given by `optim.method`

The `fkml` parameterisation `starship` uses separate (faster) code. See `fit.fkml` for details.

See `GeneralisedLambdaDistribution` for details on parameterisations.

**Value**

`starship` returns an object of class "starship".

`print` prints the estimated values of the parameters, while `summary.starship` prints these by default, but can also provide details of the estimation process (from the components `grid.results`, `data` and `optim` detailed below).

An object of class "starship" is a list containing the following components:

- `lambda`: A vector of length 4 (or 5, for the fm5 parameterisation), giving the estimated parameters, in order, $\lambda_1$ - location parameter, $\lambda_2$ - scale parameter, $\lambda_3$ - first shape parameter, $\lambda_4$ - second shape parameter (See `gld` for details of the parameters in the fm5 parameterisation). In the gpd parameterisation, the parameters are labelled: $\alpha$ - location parameter, $\beta$ - scale parameter, $\delta$ - skewness parameter, $\lambda$ - tailweight parameter.

- `grid.results`: output from the grid search - see `starship.adaptivegrid` for details.

- `optim`: output from the optim search - `optim` for details.

- `data`: The data, if `return.data` is TRUE.

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**References**


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**See Also**

`starship.adaptivegrid`, `starship.obj`
Examples

data <- rgl(100,0,1,2,2)
starship(data, optim.method = "Nelder-Mead", initgrid = list(lcvect = (0:4)/10,
ldvect = (0:4)/10))

starship.adaptivegrid  Carry out the “starship” estimation method for the generalised lambda distribution using a grid-based search

Description

Calculates estimates for the generalised lambda distribution on the basis of data, using the starship method. The starship method is built on the fact that the generalised lambda distribution (gld) is a transformation of the uniform distribution. This method finds the parameters that transform the data closest to the uniform distribution. This function uses a grid-based search.

Usage

starship.adaptivegrid(data, initgrid, inverse.eps = 1e-08, param = "FMKL")

Arguments

data          Data to be fitted, as a vector
initgrid      A list with elements, lcvect, a vector of values for \(\lambda_3\), ldvect, a vector of values for \(\lambda_4\) and levect, a vector of values for \(\lambda_5\) (levect is only required if param is fm5). The parameter values given in initgrid are not checked with gl.check.lambda.
inverse.eps   Accuracy of calculation for the numerical determination of \(F(x)\), defaults to \(10^{-8}\)

Details

The starship method is described in King \& MacGillivray, 1999 (see references). It is built on the fact that the generalised lambda distribution (gld) is a transformation of the uniform distribution. Thus the inverse of this transformation is the distribution function for the gld. The starship method applies different values of the parameters of the distribution to the distribution function, calculates the depths \(q\) corresponding to the data and chooses the parameters that make the depths closest to a uniform distribution.

The closeness to the uniform is assessed by calculating the Anderson-Darling goodness-of-fit test on the transformed data against the uniform, for a sample of size \(\text{length(data)}\).

This function carries out a grid-based search. This was the original method of King \& MacGillivray, 1999, but you are advised to instead use starship which uses a grid-based search together with an optimisation based search.

See GeneralisedLambdaDistribution for details on parameterisations.
Value

response  The minimum “response value” — the result of the internal goodness-of-fit measure. This is the return value of starship.obj. See King & MacGillivray, 1999 for more details

lambda  A vector of length 4 giving the values of \(\lambda_1\) to \(\lambda_4\) that produce this minimum response, i.e. the estimates

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See Also

starship, starship.obj

Examples

data <- rgl(100,0,1:2)
starship.adaptivegrid(data, list(lcvec=(0:4)/10, ldvec=(0:4)/10))

starship.obj  Objective function that is minimised in starship estimation method

Description

The starship is a method for fitting the generalised lambda distribution. See starship for more details.

This function is the objective function minimised in the methods. It is a goodness of fit measure carried out on the depths of the data.

Usage

starship.obj(par, data, inverse.eps, param = "fml")
Arguments

par parameters of the generalised lambda distribution, a vector of length 4, giving \( \lambda_1 \) to \( \lambda_4 \). See GeneralisedLambdaDistribution for details on the definitions of these parameters.

data Data — a vector.

inverse.eps Accuracy of calculation for the numerical determination of \( F(x) \), defaults to \( 10^{-8} \).


Details

The starship method is described in King \& MacGillivray, 1999 (see references). It is built on the fact that the generalised lambda distribution (gld) is a transformation of the uniform distribution. Thus the inverse of this transformation is the distribution function for the gld. The starship method applies different values of the parameters of the distribution to the distribution function, calculates the depths \( q \) corresponding to the data and chooses the parameters that make the depths closest to a uniform distribution.

The closeness to the uniform is assessed by calculating the Anderson-Darling goodness-of-fit test on the transformed data against the uniform, for a sample of size length(data).

This function returns that objective function. It is provided as a separate function to allow users to carry out minimisations using optim or other methods. The recommended method is to use the starship function.

Value

The Anderson-Darling goodness of fit measure, computed on the transformed data, compared to a uniform distribution. Note that this is NOT the goodness-of-fit measure of the generalised lambda distribution with the given parameter values to the data.

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References


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See Also

starship, starship.adaptivegrid

Examples

data <- rgl(100, 0, 1, 2, 2)
starship.obj(c(0, 1, 2, 2), data, inverse.eps=1e-10, "fmkl")
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