

Package ‘CreditRisk’

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at1p	<i>Analytically - Tractable First Passage (ATIP) model</i>
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Description

at1p calculates the survival probability $Q(\tau > t)$ and default intensity for each maturity according to the structural Analytically - Tractable First Passage model.

Usage

at1p(V0, H0, B, sigma, r, t)

Arguments

V0	firm value at time $t = 0$ (it is a constant value).
H0	value of the safety level at time $t = 0$.
B	free positive parameter used for shaping the barrier H_t .
sigma	a vector of constant stepwise volatility σ_t .
r	a vector of constant stepwise risk-free rate.
t	a vector of debt maturity structure (it is a numeric vector).

Details

In this function the safety level H_t is calculated using the formula:

$$H(t) = \frac{H0}{V0} * E_0[V_t] * \exp^{-B \int_0^t \sigma_u du}$$

The backbone of the default barrier at t is a proportion, controlled by the parameter $H0$, of the expected value of the company assets at t . $H0$ may depend on the level of the liabilities, on safety covenants, and in general on the characteristics of the capital structure of the company. Also, depending on the value of the parameter B , it is possible that this backbone is modified by accounting for the volatility of the company assets. For example, if $B > 0$ corresponds to the interpretation that when volatility increases - which can be independent of credit quality - the barrier is slightly lowered to cut some more slack to the company before going bankrupt. When $B = 0$ the barrier does not depend on the volatility and the "distance to default" is simply modelled through the barrier parameter $H0$.

Value

at1p returns an object of class `data.frame` containing the firm value, safety level $H(t)$ and the survival probability for each maturity. The last column is the default intensity calculated among each interval Δt .

References

Damiano Brigo, Massimo Morini, Andrea Pallavicini (2013) Counterparty Credit Risk, Collateral and Funding. With Pricing Cases for All Asset Classes.

Examples

```
mod <- at1p(V0 = 1, H0 = 0.7, B = 0.4, sigma = rep(0.1, 10), r = cdsdata$ED.Zero.Curve,
t = cdsdata$Maturity)
mod

plot(cdsdata$Maturity, mod$Ht, type = 'b', xlab = 'Maturity', ylab = 'Safety Level H(t)',
main = 'Safety level for different maturities', ylim = c(min(mod$Ht), 1.5),
col = 'red')
lines(cdsdata$Maturity, mod$Vt, xlab = 'Maturity', ylab = 'V(t)',
main = 'Value of the Firm \n at time t', type = 's')

plot(cdsdata$Maturity, mod$Survival, type = 'b',
main = 'Survival Probability for different Maturity \n (AT1P model)',
xlab = 'Maturity', ylab = 'Survival Probability')

matplot(cdsdata$Maturity, mod$Default.Intensity, type = 'l', xlab = 'Maturity',
ylab = 'Default Intensity')
```

BlackCox

Black and Cox's model

Description

BlackCox calculates the survival probability $Q(\tau > t)$ and default intensity for each maturity according to the structural Black and Cox's model.

Usage

```
BlackCox(L, K = L, V0, sigma, r, gamma, t)
```

Arguments

L	debt face value at maturity $t = T$ (it is a constant value).
K	positive parameter needed to calculate the safety level.
V0	firm value at time $t = 0$ (it is a constant value).
sigma	volatility (constant for all t).

r	risk-free rate (constant for all t).
gamma	interest rate used to discount the safety level H_t (it is a constant value).
t	a vector of debt maturity structure (it is a numeric vector).

Details

In Merton's model the default event can occur only at debt maturity T while in Black and Cox's model the default event can occur even before. In this model the safety level is given by the output H_t . Hitting this barrier is considered as an earlier default. Assuming a debt face value of L at the final maturity that coincides with the safety level in $t = T$, the safety level in $t \leq T$ is the K , with $K \leq L$, value discounted at back at time t using the interest rate γ , obtaining:

$$H(t|t \leq T) = K * \exp^{-\gamma*(T-t)}$$

The output parameter `Default.Intensity` represents the default intensity of Δt . The firm's value V_t is calculated as in the Merton function.

Value

This function returns an object of class `data.frame` containing firm value, safety level $H(t)$ and the survival probability for each maturity. The last column is the default intensity calculated among each interval Δt .

References

David Lando (2004) Credit risk modeling.

Damiano Brigo, Massimo Morini, Andrea Pallavicini (2013) Counterparty Credit Risk, Collateral and Funding. With Pricing Cases for All Asset Classes.

Examples

```
mod <- BlackCox(L = 0.55, K = 0.40, V0 = 1, sigma = 0.3, r = 0.05, gamma = 0.04,
t = c(0.50, 1.00, 2.00, 5.00, 7.00, 10.00, 20.00, 30.00))
mod

plot(c(0.50, 1.00, 2.00, 5.00, 7.00, 10.00, 20.00, 30.00), mod$Ht, type = 'b',
xlab = 'Maturity', ylab = 'Safety Level H(t)', main = 'Safety level for different
maturities', ylim = c(min(mod$Ht), 1.5), col = 'red')
abline(h = 0.55, col = 'red')
lines(c(0.50, 1.00, 2.00, 5.00, 7.00, 10.00, 20.00, 30.00), mod$Vt, xlab = 'Maturity',
ylab = 'V(t)', main = 'Value of the Firm \n at time t', type = 's')

plot(c(0.50, 1.00, 2.00, 5.00, 7.00, 10.00, 20.00, 30.00), mod$Survival, type = 'b',
main = 'Survival Probability for different Maturity \n (Black & Cox model)',
xlab = 'Maturity', ylab = 'Survival Probability')

matplot(c(0.50, 1.00, 2.00, 5.00, 7.00, 10.00, 20.00, 30.00), mod$Default.Intensity,
type = 'l', xlab = 'Maturity', ylab = 'Default Intensity')
```

calibrate.at1p	ATIP model calibration to market CDS data
----------------	---

Description

Compares CDS rates quoted on the market with theoretic CDS rates calculated by the function `cds` and looks for the parameters to be used into `at1p` for returning the default intensities corresponding to real market CDS rates performing the minimization of the objective function.

Usage

```
calibrate.at1p(V0, cdsrate, r, t, ...)
```

Arguments

<code>V0</code>	firm value at time $t = 0$.
<code>cdsrate</code>	CDS rates from market.
<code>r</code>	a vector of risk-free rate.
<code>t</code>	a vector of debt maturity structure.
<code>...</code>	additional parameters used in <code>cds</code> function.

Details

Inside `calibrate.at1p`, the function `objfn` takes the input a vector of parameters and returns the mean error occurred estimating CDS rates with `cds` function. The inputs used in `cds` are the default intensities calculated by the `at1p` function with the calibrated parameters. In particular the error is calculated as:

$$\frac{1}{n} \sum_{i=1}^n (e^{ds} - c_{mkt}^{ds})^2.$$

This quantity is a function of the default intensities and it is the objective function to be minimized in order to take optimal solutions for intensities.

Value

`calibrate.at1p` returns an object of class `data.frame` with calculated parameters of the `at1p` model and the error occurred in the minimization procedure.

References

Damiano Brigo, Massimo Morini, Andrea Pallavicini (2013) Counterparty Credit Risk, Collateral and Funding. With Pricing Cases for All Asset Classes

Examples

```
calibrate.at1p(V0 = 1, cdsrate = cdsdata$Par.spread, r = cdsdata$ED.Zero.Curve,
t = cdsdata$Maturity)
```

calibrate.BlackCox *Black and Cox model calibration to market CDS data*

Description

Compares CDS rates quoted on the market with theoretic CDS rates calculated by the function `cds` and looks for the parameters to be used into `BlackCox` for returning the default intensities corresponding to real market CDS rates performing the minimization of the objective function.

Usage

```
calibrate.BlackCox(V0, cdsrate, r, t, ...)
```

Arguments

<code>V0</code>	firm value at time $t = 0$.
<code>cdsrate</code>	CDS rates from the market.
<code>r</code>	risk-free rate.
<code>t</code>	a vector of debt maturity structure.
<code>...</code>	additional parameters used in <code>cds</code> function.

Details

Inside `calibrate.BlackCox`, the function `objfn` takes the input a vector of parameters and returns the mean error occurred estimating CDS rates with `cds` function. The inputs used in `cds` are the default intensities calculated by the `BlackCox` function with the calibrated parameters. In particular the error is calculated as:

$$\frac{1}{n} \sum_{i=1}^n (e^{ds} - c_{mkt}^{ds})^2.$$

This quantity is a function of the default intensities and it is the objective function to be minimized in order to take optimal solutions for intensities.

Value

`calibrate.BlackCox` returns an object of class `data.frame` with calculated parameters of the `BlackCox` model and the error occurred in the minimization procedure.

References

Damiano Brigo, Massimo Morini, Andrea Pallavicini (2013) Counterparty Credit Risk, Collateral and Funding. With Pricing Cases for All Asset Classes

Examples

```
calibrate.BlackCox(V0 = 1, cdsrate = cdsdata$Par.spread, r = 0.005, t = cdsdata$Maturity)
```

calibrate.cds	<i>Calibrate the default intensities to market CDS data</i>
---------------	---

Description

Compares CDS rates quoted on market with theoretic CDS rates and looks for default intensities that correspond to real market CDS rates through a minimization problem of an objective function.

Usage

```
calibrate.cds(r, t, Tj, cdsrate, ...)
```

Arguments

r	interest rates.
t	premiums timetable.
Tj	CDS maturities.
cdsrate	CDS rates from market.
...	additional parameters used in cds function.

Details

Inside `calibrate.cds`, the function `err.cds` takes the input a vector of intensities and return the mean error occurred estimating CDS rates with `cds`. In particular such error is calculated as:

$$\frac{1}{n} \sum_{i=1}^n (c^{ds} - c_{mkt}^{ds})^2.$$

This quantity is a function of default intensities and is the our objective function to be minimized in order to take optimal solutions for intensities.

Value

returns an object of class `list` with calculated intensities and the error occurred in the minimization procedure.

References

David Lando (2004) Credit risk modeling

Damiano Brigo, Massimo Morini, Andrea Pallavicini (2013) Counterparty Credit Risk, Collateral and Funding. With Pricing Cases for All Asset Classes

Examples

```
calibrate.cds( r = cdsdata$ED.Zero.Curve, t = seq(.5, 30, by = 0.5),
              Tj = c(1, 2, 3, 4, 5, 7, 10, 20, 30), cdsrate = cdsdata$Par.spread, RR = 0.4)
```

 calibrate.sbtv

SBTV model calibration to market CDS data

Description

Compares CDS rates quoted on the market with theoretic CDS rates calculated by the function `cds` and looks for the parameters to be used into `sbtv` for returning the default intensities corresponding to real market CDS rates performing the minimization of the objective function.

Usage

```
calibrate.sbtv(V0, p, cdsrate, r, t, ...)
```

Arguments

<code>V0</code>	firm value at time $t = 0$.
<code>p</code>	vector of the probability of different scenario (sum of <code>p</code> must be 1).
<code>cdsrate</code>	CDS rates from market.
<code>r</code>	a vector of risk-free rate.
<code>t</code>	a vector of debt maturity structure.
<code>...</code>	additional parameters used in <code>cds</code> function.

Details

Inside `calibrate.sbtv`, the function `objfn` takes the input a vector of parameters and returns the mean error occurred estimating CDS rates with `cds` function. The inputs used in `cds` are the default intensities calculated by the `sbtv` function with the calibrated parameters. In particular the error is calculated as:

$$\frac{1}{n} \sum_{i=1}^n (c^{ds} - c_{mkt}^{ds})^2.$$

This quantity is a function of the default intensities and it is the objective function to be minimized in order to take optimal solutions for intensities.

Value

This function returns an object of class `list` with calculated parameters of `sbtv` model and the error occurred in the minimization procedure.

References

Damiano Brigo, Massimo Morini, Andrea Pallavicini (2013) Counterparty Credit Risk, Collateral and Funding. With Pricing Cases for All Asset Classes

Examples

```
calibrate.sbtv(V0 = 1, p = c(0.95, 0.05), cdsrate = cdsdata$Par.spread,
r = cdsdata$ED.Zero.Curve, t = cdsdata$Maturity)
```

cbs

*Calculates Credit Default Swap rates***Description**

Calculates CDS rates starting from default intensities.

Usage

```
cbs(t, int, r, R = 0.005, RR = 0.4, simplified = FALSE)
```

Arguments

t	premium timetable.
int	deterministic default intensities vector.
r	spot interest rates.
R	constant premium payments, value that the buyer pays in each t_i .
RR	recovery rate on the underline bond, default value is 40%.
simplified	logic argument. If FALSE calculates the CDS rates using the simplified version of calculations, if TRUE use the complete version.

Details

- Premium timetable is $t_i; i = 1, \dots, T$. The vector starts from $t_1 \leq 1$, i.e. the first premium is paid at a year fraction in the possibility that the bond is not yet defaulted. Since premium are a postponed payment (unlike usual insurance contracts).
- Intensities timetable have domains $\gamma_i; i = t_1, \dots, T$.
- spot interest rates of bond have domain $r_i; i = t_1, \dots, T$. The function transforms spot rates in forward rates. If we specify that we want to calculate CDS rates with the simplified algorithm, in each period, the amount of the constant premium payment is expressed by:

$$\pi^{pb} = \sum_{i=1}^T p(0, i) S(0, i) \alpha_i$$

and the amount of protection, assuming a recovery rate δ , is:

$$\pi^{ps} = (1 - \delta) \sum_{i=1}^T p(0, i) \hat{Q}(\tau = i) \alpha_i$$

If we want to calculate same quantities with the complete version, that evaluate premium in the continuous, the value of the premium leg is calculated as:

$$\pi^{pb}(0,1) = - \int_{T_a}^{T_b} P(0,t) \cdot (t - T_{\beta(t)-1}) d_t Q(\tau \geq t) + \sum_{i=a+1}^b P(0, T_i) \cdot \alpha_i * Q(\tau \geq T_i)$$

and the protection leg as:

$$\pi_{a,b}^{ps}(1) := - \int_{t=T_a}^{T_b} P(0,t) d * Q(\tau \geq t)$$

In both versions the forward rates and intensities are supposed as constant stepwise functions with discontinuity in t_i

Value

cds returns an object of class `data.frame` with columns, for each date t_i the value of survival probability, the premium and protection leg, CDS rate and CDS price.

References

David Lando (2004) Credit risk modeling.

Damiano Brigo, Massimo Morini, Andrea Pallavicini (2013) Counterparty Credit Risk, Collateral and Funding. With Pricing Cases for All Asset Classes

Examples

```
cds(t = seq(0.5, 10, by = 0.5), int = seq(.01, 0.05, len = 20),
r = seq(0,0.02, len=20), R = 0.005, RR = 0.4, simplified = FALSE)
```

cds2

Calculate Credit Default Swap rates

Description

Calculate CDS rates starting from default intensities

Usage

```
cds2(t, Tj, tr, r, tint, int, R = 0.005, ...)
```

Arguments

t	premium timetable.
Tj	CDS maturities.
tr	interest rates timetable.
r	spot interest rates.
tint	intensity timetable.
int	default intensities timetable.
R	constant premium payment.
...	further arguments on cds.

Details

The function `cds2` is based on `cds` but allows a more fine control on maturities and on discretization of `r` and `int`. In particular input (`t`, `tr`, `tint`) can be of different length thanks to the function [approx](#).

Value

An object of class `data.frame` that contains the quantities calculated by `cds` on `Tj` timetable.

References

David Lando (2004) Credit Risk Modeling.

Damiano Brigo, Massimo Morini, Andrea Pallavicini (2013) Counterparty Credit Risk, Collateral and Funding. With Pricing Cases for All Asset Classes

Examples

```
cds2(t = c(1:20), Tj = c(1:20), tr = c(1:20), r = seq(0.01, 0.06, len = 20),
    tint = c(1:20), int = seq(0.01, 0.06, len = 20))
```

cdsdata

CDS quotes from market

Description

- **Maturity:** Maturities of cds contracts expressed in years;
- **Par . Spread:** CDS rates quotes, spread that nullify the present value of the two legs;
- **ED . Zero . Curve:** EURIBOR interest rates (risk-free)

Usage

```
data(cdsdata)
```

Format

An object of class "data.frame".

Source

Thomson Reuters, CDS quotes of Unicredit on 2017-01-23

cum_normal_density *Cumulative Normal Distribution Function*

Description

This function calculates the cumulative normal distribution function (CDF) for a given value x using the Hastings approximation method. This approximation is typically used in finance for the calculation of option pricing probabilities.

Usage

```
cum_normal_density(x)
```

Arguments

x A numeric value or vector for which the cumulative normal distribution is to be calculated.

Details

The function uses a polynomial approximation as described by E.G. Haug in "The Complete Guide to Option Pricing Formulas" to estimate the CDF of a normal distribution. The coefficients used in the approximation are specifically chosen to minimize the error in the tail of the distribution, which is critical for financial applications like option pricing.

The polynomial approximation is applied to the normal density function:

$$N(x) = \frac{1}{\sqrt{2\pi}} e^{-x^2/2}$$

Then, the cumulative probability is adjusted based on the sign of x : - If x is non-negative, it returns $\backslash(1 - t)$, where t is the polynomial approximation. - If x is negative, it returns $\backslash(t)$.

The cumulative normal distribution function is important in statistics for hypothesis testing and in finance for the Black-Scholes option pricing formula.

Value

Returns the cumulative probability under the normal curve from $\backslash(-$

∞

$\backslash)$ to x .

References

Haug, E.G., The Complete Guide to Option Pricing Formulas. Hastings, C. Approximations for Digital Computers. Princeton Univ. Press, 1955.

Examples

```
cum_normal_density(1.96)
cum_normal_density(-1.96)
```

```
generalized_black_scholes
```

Generalized Black-Scholes Option Pricing Model

Description

This function calculates the price of a European call or put option using the generalized Black-Scholes formula, which extends the standard model to incorporate a continuous dividend yield.

Usage

```
generalized_black_scholes(TypeFlag = c("c", "p"), S, X, Time, r, b, sigma)
```

Arguments

TypeFlag	A character vector indicating the type of option to be priced, either "c" for call options or "p" for put options.
S	Current stock price (scalar).
X	Strike price of the option (scalar).
Time	Time to expiration of the option (in years).
r	Risk-free interest rate (annualized).
b	Cost of carry rate, $b = r - q$ for a dividend yield q .
sigma	Volatility of the underlying asset (annualized).

Details

The generalized Black-Scholes formula considers both the risk-free rate and a cost of carry, making it suitable for a wider range of financial instruments, including commodities and currencies with continuous yields.

The pricing formula for call and put options is determined by:

$$C = Se^{(b-r)T} N(d_1) - Xe^{-rT} N(d_2)$$

$$P = Xe^{-rT} N(-d_2) - Se^{(b-r)T} N(-d_1)$$

where:

$$d_1 = \frac{\log(S/X) + (b + \sigma^2/2)T}{\sigma\sqrt{T}}$$

$$d_2 = d_1 - \sigma\sqrt{T}$$

and $(N(\cdot))$ is the cumulative normal distribution function, estimated by the ‘cum_normal_density’ function.

Value

Returns the price of the specified option (call or put).

References

Haug, E.G., The Complete Guide to Option Pricing Formulas.

Examples

```
# Calculate the price of a call option
generalized_black_scholes("c", S = 100, X = 100, Time = 1, r = 0.05, b = 0.05, sigma = 0.2)
# Calculate the price of a put option
generalized_black_scholes("p", S = 100, X = 100, Time = 1, r = 0.05, b = 0.05, sigma = 0.2)
```

Merton

Merton's model

Description

Merton calculates the survival probability $Q(\tau > T)$ for each maturity according to the structural Merton's model.

Usage

```
Merton(L, V0, sigma, r, t)
```

Arguments

L	debt face value at maturity $t = T$; if the value of the firm V_T is below the debt face value to be paid in T the company default has occurred (it is a constant value).
V0	firm value at time $t = 0$ (it is a constant value).
sigma	volatility (constant for all t).
r	risk-free rate (constant for all t).
t	a vector of debt maturity structure. The last value of this vector represents the debt maturity T .

Details

In Merton model the default event can occur only at debt maturity T and not before. In this model the debt face value L represents the constant safety level. In this model the firm value is the sum of the firm equity value S_t and the firm debt value D_t . The debt value at time $t < T$ is calculated by the formula:

$$D_t = L * \exp(-r(T - t)) - Put(t, T; V_t, L)$$

The equity value can be derived as a difference between the firm value and the debt:

$$S_t = V_t - D_t = V_t - L * \exp(-r(T - t)) + Put(t, T; V_t, L) = Call(t, T; V_t, L)$$

(by the put-call parity) so that in the Merton model the equity can be interpreted as a Call option on the value of the firm.

Value

Merton returns an object of class `data.frame` with:

- `Vt`: expected Firm value at time $t < T$ calculated by the simple formula $V_t = V_0 * \exp(rt)$.
- `St`: firm equity value at each $t < T$. This value can be seen as a call option on the firm value `V_t`.
- `Dt`: firm debt value at each $t < T$.
- `Survival`: survival probability for each maturity.

References

Damiano Brigo, Massimo Morini, Andrea Pallavicini (2013) Counterparty Credit Risk, Collateral and Funding. With Pricing Cases for All Asset Classes

Examples

```
mod <- Merton(L = 10, V0 = 20, sigma = 0.2, r = 0.005,
             t = c(0.50, 1.00, 2.00, 3.25, 5.00, 10.00, 15.00, 20.00))
mod

plot(c(0.50, 1.00, 2.00, 3.25, 5.00, 10.00, 15.00, 20.00), mod$Surv,
     main = 'Survival Probability for different Maturity \n (Merton model)',
     xlab = 'Maturity', ylab = 'Survival Probability', type = 'b')
```

Merton.sim

Firm value in Merton's model

Description

With this function we simulate n trajectories of firm value based on Merton's model.

Usage

```
Merton.sim(V0, r, sigma, t, n, seed = as.numeric(Sys.time()))
```

Arguments

<code>V0</code>	firm value at time $t = 0$.
<code>r</code>	risk-free interest rate (constant for all t).
<code>sigma</code>	volatility (constant for all t).
<code>t</code>	a vector of debt maturity structure.
<code>n</code>	number of trajectories to be generated.
<code>seed</code>	starting seed, default seed is setted randomly.

Details

The trajectories are calculated according to the equation:

$$V_T = V_0 \exp \int_0^T d\ln V_t$$

Where we express $d\ln V_t$ using Ito's lemma to derive the differential of the logarithm of the firm value as:

$$d\ln V_t = \left(\mu - \frac{\sigma^2}{2}\right)dt + \sigma dW_t$$

Value

This function returns a matrix containing the simulated firm values.

References

Gergely Daróczi, Michael Puhle, Edina Berlinger, Péter Csòka, Dániel Havran Márton Michaletzky, Zsolt Tulasay, Kata Váradi, Agnes Vidovics-Dancs (2013) Introduction to R for Quantitative Finance.

Examples

```
V <- Merton.sim(V0 = 20, r = 0.05, sigma = 0.2, t = seq(0, 30, by = 0.5), n = 5)
matplot(x = seq(0, 30, by = 0.5), y = V, type = 's', lty = 1, xlab = 'Time',
ylab = 'Firm value trajectories', main = "Trajectories of the firm values in the Merton's model")
```

sbtv

Scenario Barrier Time-Varying Volatility ATIP model

Description

sbtv calculates the survival probability $Q(\tau > t)$ and default intensity for each maturity according to the structural SBTV model.

Usage

```
sbtv(V0, H, p, B, sigma, r, t)
```


Arguments

V_0	firm value at time $t = 0$ (it is a constant value).
H	vector of different safety level at time $t = 0$.
p	vector of the probability of different scenario (sum of p must be 1).
B	free positive parameter used for shaping the barrier H_t .
σ	a vector of constant stepwise volatility σ_t .
r	a vector of constant stepwise risk-free rate.
t	a vector of debt maturity structure (it is a numeric vector).

Details

sbtv is an extension of the at1p model. In this model the parameter H_0 used in the at1p model is replaced by a random variable assuming different values in different scenarios, each scenario with a different probability. The survival probability is calculated as a weighted average of the survival probability using the formula:

$$SBTV.Surv = \sum_{i=1}^N p[i] * AT1P.Surv(H[i])$$

where $AT1P.Surv(H[i])$ is the survival probability computed according to the AT1P model when $H_0 = H[i]$ and with weights equal to the probabilities of the different scenarios.

Value

sbtv returns an object of class `data.frame` containing the survival probability for each maturity. The last column is the default intensity calculated among each interval Δt .

References

Damiano Brigo, Massimo Morini, Andrea Pallavicini (2013) Counterparty Credit Risk, Collateral and Funding. With Pricing Cases for All Asset Classes.

Examples

```
mod <- sbtv(V0 = 1, H = c(0.4, 0.8), p = c(0.95, 0.05), B = 0, sigma = rep(0.20, 10),
           r = cdsdata$ED.Zero.Curve, t = cdsdata$Maturity)

mod

plot(cdsdata$Maturity, mod$Survival, type = 'b')
```

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